

# SOLUTION

## EXAMINATION IN : MNFFY 221/SIF 4082 Energy and Environmental Physics

Monday 3. December 2001

### Problem 1

#### a) Radiative forcing

The energy balance at the top of the atmosphere requires a constant flux

$$\text{Flux out} - \text{flux in} = -\Delta I$$

Assume a doubling of the equivalent  $\text{CO}_2$  atmosphere, causes an effective reduction of the earth's long wavelength radiation, magnitude  $\Delta I$ . To compensate for this change in  $\Delta I$ , the earth temperature increase. Radiative forcing (given in  $\text{W/m}^2$ ) describe the direct effect of a change in the concentration of a specific gas or atmospheric component.

#### b)

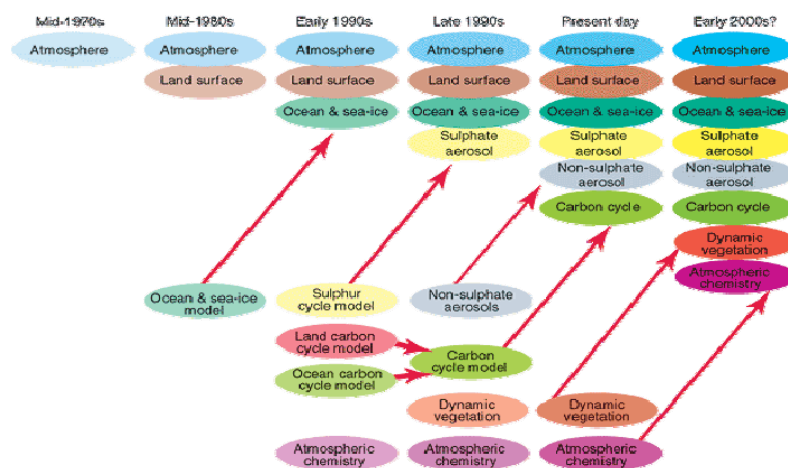
A certain change in temperature will cause a lot of effects reinforcing it. A few counteracting – thus feedback mechanisms. Some examples for the climate research

- 1) Melting of ice – snow, reduced surface albedo
- 2) Increased water vapour – smaller transmission  $t_a$  – higher backscatter
- 3) Same for increased cloud cover
- 4) a) higher sea temp gives less  $\text{CO}_2$  in ocean – higher air concentration. b) high polar temp causes decreased ocean circulation decreased  $\text{CO}_2$  absorption c) faster decay of organic material gives more  $\text{CO}_2$  and  $\text{CH}_4$
- 5) Increased  $\text{CO}_2$  increased growth reduced albedo.

#### c)

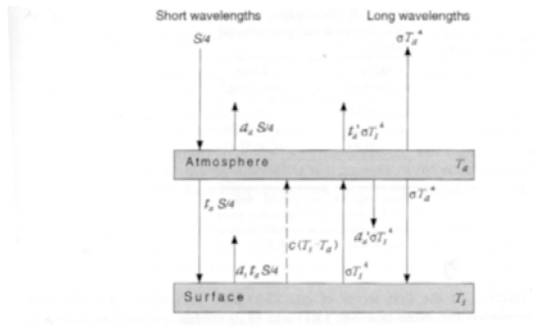
atmosphere, land surface, ocean-sea ice, sulphate aerosol, non sulphate aerosols, carbon cycle, dynamic vegetation, atmospheric chemistry.

### The Development of Climate models, Past, Present and Future



**Problem 2**

a) Fig. 3.2 in textbook (B&G) p. 31



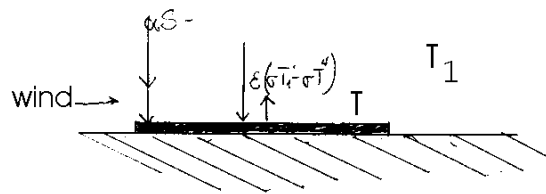
Short wavelength radiation, Long wavelength radiation, Convection

b)

Figure: describes some of the fluxes . Conduction between plate and earth is not marked on the figure.

T: surface temperature

T<sub>1</sub>: ambient temperature



$$\alpha S + \varepsilon (\sigma T_1^4 - \sigma T^4) + h_c (T_1 - T) + q_t = 0$$

$\alpha$ : Absorption coefficient for the surface, = 1 for a black surface

S: Short wave solar irradiance

$\varepsilon$ : emission coefficient for thermal radiation

$\sigma$ : Boltzmann constant

$h_c$  heat transfer number for convection depending on wind speed, for instance  $h_c = 23$  when wind speed = 5 m/s

$q_t$ : transient heat current, conduction. (relevant for bottom side of the plate)

c)

examples p. 376 in T&W)

$$E_o = \int_{z=z_1}^{z_2} \rho_r A c_r G(z-z_1) dz = \rho_r A c_r G(z_2 - z_1)^2 / 2$$

$\rho_r$ : rock density,

A: Cross section to be studied

$c_r$ : Specific heat capacity

G: temperatur gradient  $dt/dz$

z depth

$E_0$  useful heat content

ex. At 7 km the temperature  $40 \times 7 = 280$  K above the surface.

At  $140/40 = 3.5$  km there is no useful heat.

$$E_0 = 2700 \text{ [kg/m}^3\text{]} \cdot 1 \text{ km}^2 \cdot 820 \text{ [J/kg K]} \cdot (3.5)^2 \text{ [km}^2\text{]} \cdot 40/2 \text{ [K/km]} = 5.42 \cdot 10^{17} \text{ J/km}^2$$

### Problem 3

Typical structure for a solar cell:

Fig. 7.1 from T & W

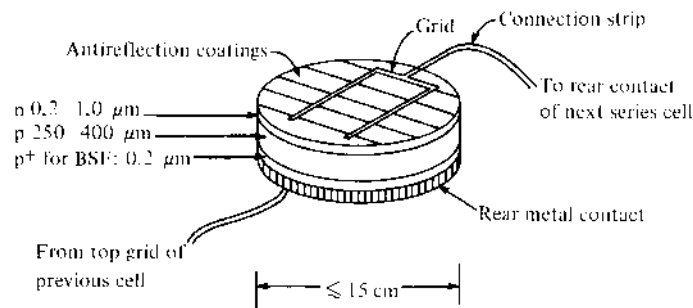


Fig. 7.1 Typical structure of n-p junction solar cell. The cover (glass or plastic) above the cell, and the filler between the cover and the cell, are not shown. BSF: back surface field

p-n junction

p and n type material (p becomes slightly negative, n positive), Voltage  $V_B$  across the junction. ( $V_B \approx 0.6V$ )

Junction currents: Generation  $I_g$  Recombination  $I_R$  (drift) ,

Biasing the material forward biasing cause a current to be run.

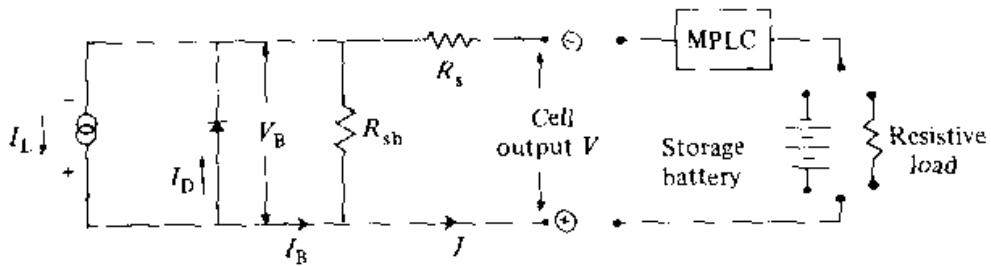
Forward bias  $I_g \ll I_R$  , Reverse bias:  $I_R = 0$

Current I is proportional with the forward biased voltage V.,  $I = I_0$  for reverse biased cell.  $I_0$  depends on temperature.

Power generation from a solar cell corresponds to conditions of diode forward bias. Potential difference across the semiconductor cell  $V_B$  is due to both forward biasing and band displacement. Will vary with the external current I. Absorption of active photons ( $h\nu > E_g$ ) to create a further current with power generating capability.

The equivalent circuit for a solar cell.

Fig 7.14 from T&W.



**Fig. 7.14** Equivalent circuit of a solar cell. Also drawn are examples of loads with maximum power load control (MPLC) to insure peak power operation

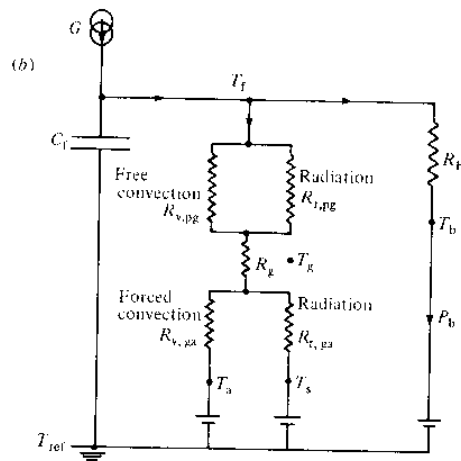
Limiting cell efficiency.

1. Top surface contact obstruction ( loss 3%)
2. Reflection at the top surface (loss 1%)
3. Photon energy less than band gap (loss 23%)
4. Excess photon energy (loss 33%)
5. Quantum efficiency (loss 0.4%)
6. Collection efficiency
7. Voltage factor (loss 22%)
8. Curve factor (loss 4%)
9. Additional curve factor A (loss 5%)
10. Series, shunt resistance,

Total efficiency: Delivered power (for Si 10-14%)

b)

Figure 5.4 (T&W)



$$R_{\text{tot}} = \{1/R_b + 1/R_{\text{pa}}\}^{-1}$$

$$R_{\text{pa}} = \{1/R_{\text{v,pg}} + 1/R_{\text{r,pg}}\}^{-1} + R_g + \{1/R_{\text{v,ga}} + 1/R_{\text{r,ga}}\}^{-1}$$

c)

Selective surfaces can be a metal-semiconductor stack.

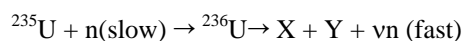
High absorption and emission in short wavelength range ( $\lambda < 3 \mu\text{m}$ ), low for thermal radiation ( $\lambda > 3 \mu\text{m}$ ).

Semiconductors are more ideal and metal. By combining both an optimum can be reached. Good conduction from the material into the metal.

#### Problem 4

a)

Dominant process



$\nu \approx 2.34$ , fast neutrons have energy on average 2 MeV, Slow neutrons are thermal  $T = 293 \text{ K}$ , Fission products can vary.

A parentheses: In real life  $^{238}\text{U}$  will also absorb neutrons, leading to  $^{239}\text{U}$  and  $^{239}\text{Np}$  to  $^{239}\text{Pu}$ .  $^{239}\text{Pu}$  is fissionable itself. At the end of the fission process it produces 50% of the fissions.  $^{239}\text{Pu}$  has different properties than  $^{235}\text{U}$ . Reactors has to be design according to their planed lifetime.

These fast neutrons has to be slowed down by a moderator material. More efficient as the mass of the moderator material reduces, thus  $\text{H}_2\text{O}$  and  $\text{D}_2\text{O}$  is mostly used.

Description of main components in the reactor.

Fig. 4.38 (B&G)

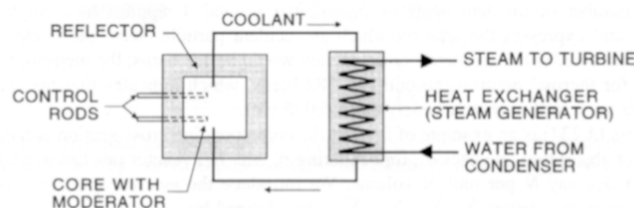


Figure 4.38 Scheme of a nuclear reactor system. The heat from the reactor core is taken away by a coolant. A reflector tries to keep as many neutrons in the core as possible, whereas control rods can absorb superfluous neutrons if necessary

b)

$\eta$ : fission yield; number of fast neutrons per slow neutron absorbed,  $\eta < \nu$ . (for instance  $\eta=1.33$ )

$$\eta = \nu \left\{ \frac{N(235)\sigma_f(235)}{[N(235)\{\sigma_f(235) + \sigma_c(235)\} + N(238)\sigma_c(238)]} \right\}$$

$\sigma_f$  cross section for slow neutron to be absorbed without fission

$\sigma_c$  cross section for slow neutron to be absorbed with fission

$\epsilon$ : the fast fission factor . Number of fast neutrons inducing a new fission in  $^{238}\text{U}$  and  $^{235}\text{U}$  or  $\epsilon$ ,  $\epsilon$  is slightly higher than 1.

p: resonance escape probability. Probability of fast neutrons not to be absorbed by  $^{238}\text{U}$  as it is slowed down by the moderator due to resonance phenomena in moderator material. p increase with less moderator material

f: thermal utilization factor. Slow neutrons absorbed by the moderator material or cladding of fuel elements. f increase with more moderator material.

The product  $pf$  has a maximum at a certain ratio between moderator material and fuel.

Number of fast neutrons will be:  $\eta\epsilon p n$ . n number of slow neutrons

A fraction of fast neutrons  $l_f$  will leak out of the reactor, leaving  $(1 - l_f)$  and similar a fraction  $l_s$  of slow neutron can leak out of the reactor  $(1 - l_s)$ , but due to the size of the reactors this effect can usually be ignored.

The total number of available slow neutrons ready for a new round of fission will be

$nk = \eta\epsilon pfn$ , k is called multiplication factor.

$k = \eta\epsilon pf$

The magnitude of k depends on the ratio of moderator material and fuel are approximately 1 (between 0.9 and 1.1)

c)

Bq: number of nucleus decaying per second [ $\text{s}^{-1}$ ]

Gy: Energy absorbed per kg [J/kg]

Sv:  $1 \text{ Gy} \cdot Q = 1 \text{ SV}$  [biological weighted J/kg]

Q: quality factor dependent on type of radiation,

Q=1 for X-rays,  $\gamma$ -rays, electrons and muons

Q=5 for neutrons with energies  $< 10 \text{ keV}$ ,  $> 20 \text{ MeV}$  and protons with energy  $> 2 \text{ MeV}$

Q=10 for neutrons with energies from  $10 \text{ keV}$  to  $100 \text{ keV}$  and  $2 \text{ MeV}$  to  $20 \text{ MeV}$

Q=20 for other neutrons and  $\alpha$ -particles and other particles with a charge larger than one

Radon is the largest health risk in Western world.